

## Multiplying Fractions

### Student Probe

There are 15 cars in Michael's toy car collection. Two thirds of the cars are red. How many red cars does Michael have?

Answer: 10 red cars

### Lesson Description

This lesson uses diagrams to help students develop a conceptual understanding of multiplying with fractions and mixed numbers.

### Rationale

It's important that students have ample opportunity to develop fraction number sense before being introduced to sets of rules. Also, students should be able to compute with fractions, primarily for the purpose of making estimations, understanding computations done with technology, and simple calculations. Since the process of multiplying rational algebraic expression is the same as the process of multiplying numerical expressions, it is essential that students can fluently multiply fractions before entering algebra courses.

### Preparation

Prepare problems for students to work.

### At a Glance

What: Multiply fractions, including mixed numbers

Common Core State Standard: CC.6.NS.1

Apply and extend previous understandings of multiplication and division to divide fractions by fractions. Interpret and compute quotients of fractions, and solve word problems involving division of fractions by fractions, e.g., by using visual fraction models and equations to represent the problem.

Matched Arkansas Standard: AR.6.NO.3.2

(NO.3.6.2) Computational Fluency:

Develop and analyze algorithms for computing with fractions (including mixed numbers) and decimals and demonstrate, with and without technology, computational fluency in their use and justify the solution

Mathematical Practices:

Make sense of problems and persevere in solving them.

Who: Students who cannot multiply fractions including mixed numbers, and students who need to build upon their ideas about whole number operations to gain meaning of fraction computation.

Grade Level: 6

Prerequisite Vocabulary: none

Prerequisite Skills: naming fractional parts, equivalent fractions, whole number multiplication

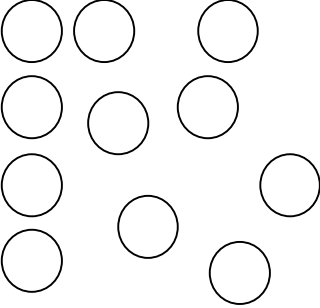
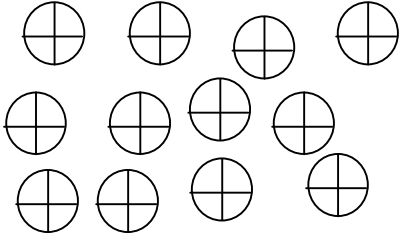
Delivery Format: individual, small group, or whole group


Lesson Length: 30 minutes

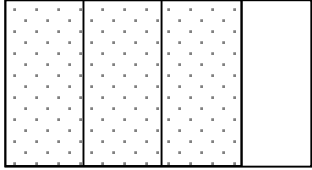
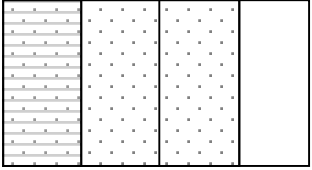
Materials, Resources, Technology: none


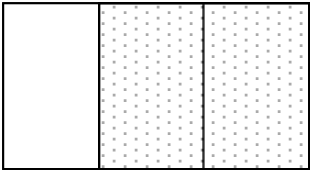
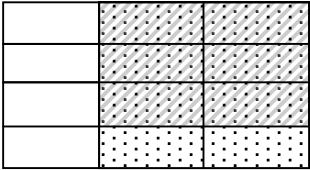
Student Worksheets: none

## Lesson

The teacher says or does...	Expect students to say or do...	If students do not, then the teacher says or does...
<p>1. Suzanne has 11 snack cakes. She wants to share them with her three friends. How many snack cakes will Suzanne and each of her three friends get?</p> <p>Let's draw a diagram to help us find the answer.</p> <p>(See Teacher Notes for an alternative method.)</p>		<p>Draw eleven snack cakes.</p>
<p>2. Since there are 4 people (Suzanne and her 3 friends), what part of each cake, will each person receive?</p> <p>Divide each snack cake into fourths in your diagram.</p>	$\frac{1}{4}$ 	<p>If 4 people wanted to share one cake, how would you divide it so that everyone received the same amount?</p>
<p>3. How many pieces are there altogether? How do you know?</p>	<p>44 pieces</p> <p>11 cakes <math>\cdot</math> 4 pieces in each cake = 44 pieces.</p>	<p>Each cake has 4 pieces and there are 11 cakes, so how many pieces altogether? OR Let's count the pieces.</p>
<p>4. How many pieces should each person receive? How do you know?</p>	<p>11 pieces</p> <p>44 pieces <math>\div</math> 4 people = 11 pieces per person.</p> $\frac{3}{4} \text{ of } \frac{2}{3} = \frac{3}{4} \cdot \frac{2}{3}$ $= \frac{\cancel{3} \cdot 2}{4 \cdot \cancel{3}}$ $= \frac{6}{12} \text{ or } \frac{1}{2}$	<p>Count with the students.</p>

The teacher says or does...	Expect students to say or do...	If students do not, then the teacher says or does...
<p>5. Now we need to figure out what part of a whole snack cake the 11 pieces represent. Let's count 11 pieces to figure it out. (Number pieces 1-11 on the diagram.)</p>	<p>4 pieces = 1 cake 4 pieces = 1 cake 3 pieces = <math>\frac{3}{4}</math> cake</p> <hr/> <p>11 pieces = <math>2\frac{3}{4}</math> cakes</p>	<p>How many whole cakes did each person receive? What part of a cake did each person receive?</p>
<p>6. Let's write a number sentence to show what we did.</p> $\frac{1}{4} \text{ of } 11 = \frac{1}{4} \cdot 11$ $= \frac{11}{4}$ $= 2 + \frac{3}{4}$ $= 2\frac{3}{4}$ <p>(Directly relate each step to the diagrams.)</p>		
<p>7. Thomas had <math>\frac{3}{4}</math> of a pizza left. He gave <math>\frac{1}{3}</math> of the leftover pizza to his brother. How much of a whole pizza did his brother get?</p> <p>Let's draw a diagram to help us find the answer.</p> <p>The rectangle represents the whole pizza.</p>		<p>Model</p>

The teacher says or does...	Expect students to say or do...	If students do not, then the teacher says or does...
<p>8. Let's represent how much of the pizza is left. How many equal sized pieces do we need to show <math>\frac{3}{4}</math>?</p> <p>Shade <math>\frac{3}{4}</math> of the rectangle.</p> <p>This represents the leftover pizza.</p>	<p>4</p> 	<p>Model</p>
<p>9. Thomas gave his brother <math>\frac{1}{3}</math> of the leftover pizza.</p> <p>Shade <math>\frac{1}{3}</math> of the leftover pizza.</p>		<p>Model</p>
<p>10. What part of the whole pizza does this represent?</p> <p>How do you know?</p>	<p><math>\frac{1}{4}</math></p> <p>The whole pizza is divided into 4 pieces, and this is 1 piece.</p>	<p>How many pieces are there altogether?</p> <p>How many pieces have been shaded twice?</p>
<p>11. Let's write a number sentence to show what we did.</p> $\frac{1}{3} \text{ of } \frac{3}{4} = \frac{1}{3} \cdot \frac{3}{4}$ $= \frac{1 \cdot \cancel{3}}{\cancel{3} \cdot 4}$ $= \frac{1}{4}$ <p>(Directly relate each step to the diagrams.)</p>		

The teacher says or does...	Expect students to say or do...	If students do not, then the teacher says or does...
<p>12. Zach had <math>\frac{2}{3}</math> of the lawn left to cut. After lunch he cut <math>\frac{3}{4}</math> of the grass he had left. How much of the whole lawn did Zack cut after lunch?</p> <p>Let's draw a diagram to help us find the answer.</p> <p>The rectangle represents the whole lawn.</p>		
<p>13. Let's represent how much of the lawn Zach had left to mow when he went to lunch. How many equal sized pieces do we need to represent <math>\frac{2}{3}</math>?</p>	<p>3</p> 	Model
<p>14. After lunch, Zach mowed <math>\frac{3}{4}</math> of the <math>\frac{2}{3}</math>. Shade <math>\frac{3}{4}</math> of the remaining lawn.</p> <p>How many equal size pieces do we need to represent <math>\frac{3}{4}</math>?</p>	<p>4</p> 	Model
<p>15. The lawn is now divided into how many pieces?</p> <p>How many pieces have been shaded twice?</p> <p>What part of the whole lawn is that?</p>	<p>12</p> <p>6</p> <p><math>\frac{6}{12}</math> or <math>\frac{1}{2}</math></p>	Count the pieces with the students.

The teacher says or does...	Expect students to say or do...	If students do not, then the teacher says or does...
<p>16. Let's write a number sentence to show what we did.</p> $\frac{3}{4} \text{ of } \frac{2}{3} = \frac{3}{4} \cdot \frac{2}{3}$ $= \frac{3 \cdot 2}{4 \cdot 3}$ $= \frac{6}{12} \text{ or } \frac{1}{2}$ <p>(Directly relate each step to the diagrams.)</p>		

### Teacher Notes

1. Diagrams should be used extensively before the computational algorithm is introduced.
2. When drawing diagrams to represent fractions, rectangles are easier to subdivide than circles.
3. Every effort should be made to relate the number sentences to the diagrams.
4. As an alternative method for solving Suzanne's snack cake problem, share the whole cakes among the four people (each receives 2 whole cakes) and divide the remaining 3 cakes equally among the 4 (each receives  $\frac{3}{4}$  of a cake more).
5. Once students have explored products with factors less than one, it may be challenging to have them see if they can use a similar type drawing to explain products with either or both factors great than 1. Diagrams should be used before the computational algorithm is introduced.
6. Problems should progress from unit parts without subdivisions (Thomas' pizza problem) to unit parts with subdivisions (Zach's mowing problem).

### **Variations**

None

## Formative Assessment

Someone ate  $\frac{1}{10}$  of the cake, leaving only  $\frac{9}{10}$ . If you eat  $\frac{2}{3}$  of the cake that is left, how much of the whole cake will you have eaten?

Answer:  $\frac{18}{30}$  or  $\frac{3}{5}$ .

## References

Marjorie Montague, Ph.D. (2004, 12 7). *Math Problem Solving for Middle School Students With Disabilities*. Retrieved 4 25, 2011, from The Iris Center:

[http://iris.peabody.vanderbilt.edu/resource\\_infoBrief/k8accesscenter\\_org\\_training\\_resources\\_documents\\_Math\\_Problem\\_Solving\\_pdf.html](http://iris.peabody.vanderbilt.edu/resource_infoBrief/k8accesscenter_org_training_resources_documents_Math_Problem_Solving_pdf.html)

*Mathematics Preparation for Algebra*. (n.d.). Retrieved 12 10, 2010, from Doing What Works:

[http://dww.ed.gov/practice/?T\\_ID=20&P\\_ID=48](http://dww.ed.gov/practice/?T_ID=20&P_ID=48)

Van De Walle, John A. *Elementary and Middle School Mathematics: Teaching Developmentally*. Boston: Allyn and Bacon, 2004. Print.